

Modelling human endurance: Power laws vs critical power

J. Drake A. Finke R. Ferguson

School of Science

June 28, 2023

Outline



Background

- Modelling human endurance

- Hyperbolic/Critical-power model

- Power-law model

Hyperbolic/Critical-power vs Power-law model

- Time to exhaustion at different powers

- Large data studies

- Summary

FTP

Summary

Modelling human endurance



Why do we care?

Modelling human endurance



Why do we care?

- ▶ **Predict** performance over a untested duration

Modelling human endurance

Why do we care?

- ▶ **Predict** performance over a untested duration

- ▶ **Assess** fitness

Modelling human endurance

Why do we care?

- ▶ **Predict** performance over a untested duration
- ▶ **Assess** fitness
- ▶ **Optimise** pacing/race strategies

Modelling human endurance

Why do we care?

- ▶ **Predict** performance over a untested duration
- ▶ **Assess** fitness
- ▶ **Optimise** pacing/race strategies

What approaches are there?

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Summary

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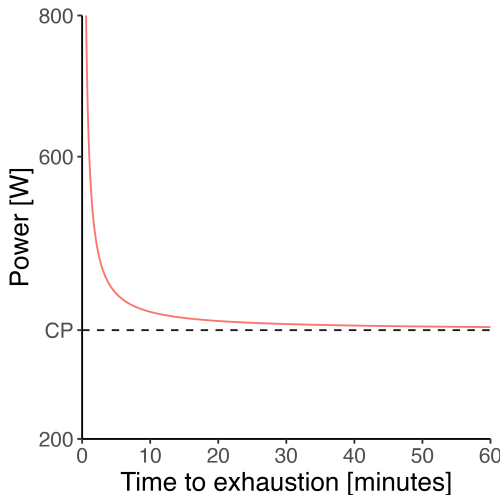
Summary

Hyperbolic/Critical-power model



What do **CP** and **W'** imply?

Hyperbolic/Critical-power model



Parameters



CP - Critical power

Parameters



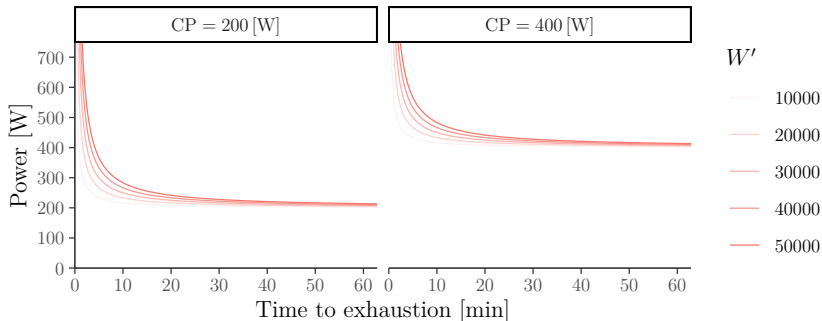
CP - Critical power

W' - The finite amount of work that can be done above CP

Parameters

CP - Critical power

W' - The finite amount of work that can be done above CP



History

Hill (1925); Jones et al. (2019); Monod and Scherrer (1965)

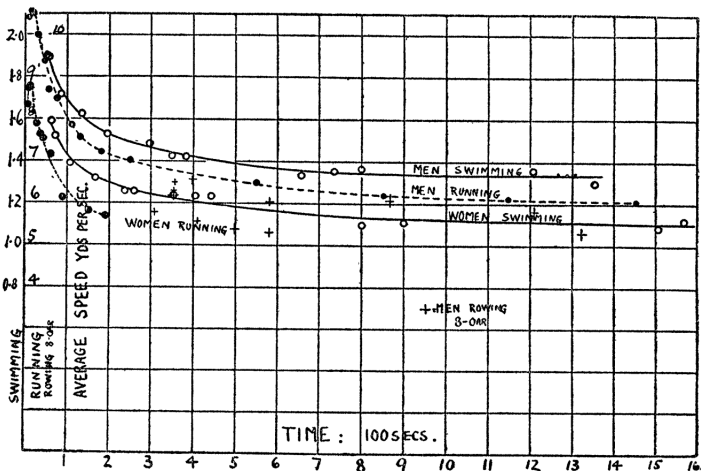


Figure: World records across different athletes (Hill, 1925)

Outline



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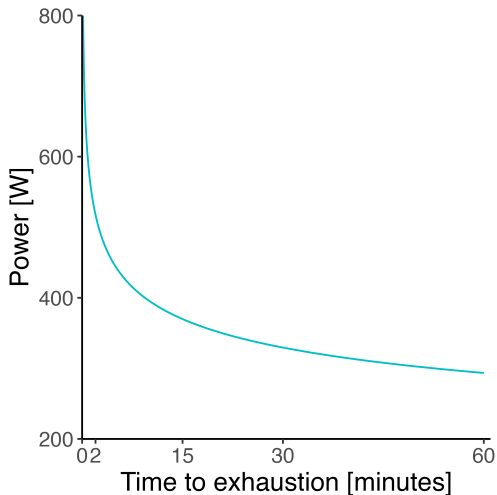
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Summary

FTP

Summary

Power-law model



Parameters



Speed, $\mathbf{S} > 0$, in cycling the theoretical 1 second power output

Parameters

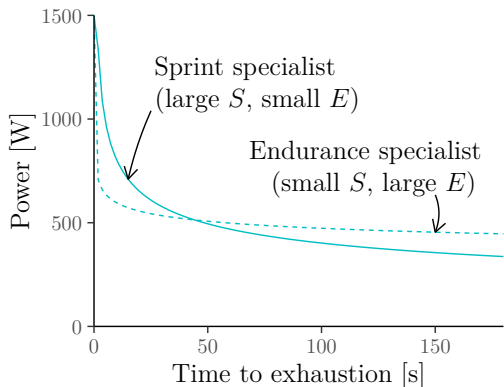
Speed, $\mathbf{S} > 0$, in cycling the theoretical 1 second power output

Endurance, $0 < \mathbf{E} < 1$, governs how quickly the power–duration curve decays

Parameters

Speed, $S > 0$, in cycling the theoretical 1 second power output

Endurance, $0 < E < 1$, governs how quickly the power–duration curve decays



History

Kennelly (1906); Riegel (1981)

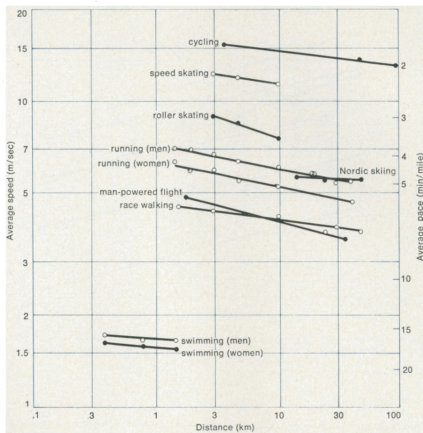


Figure: World records across different athletes from multiple sports (Riegel, 1981)

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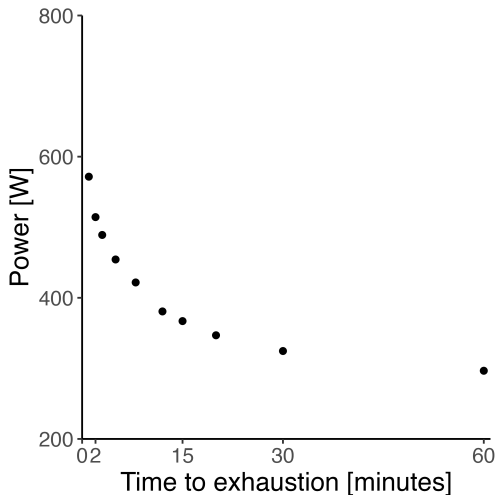
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Summary

FTP

Summary

Power–duration data



Hyperbolic/Critical-power model

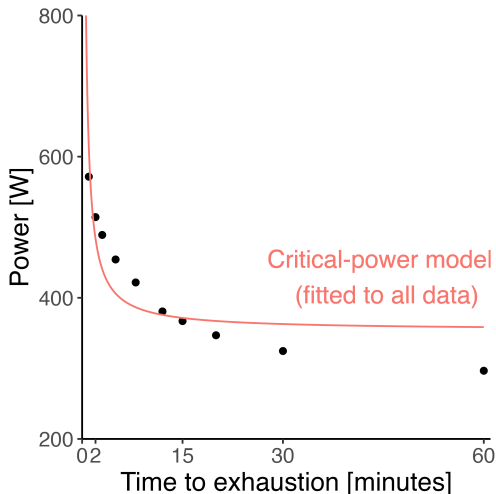


Figure: Fits poorly when applied to all data

Hyperbolic/Critical-power model

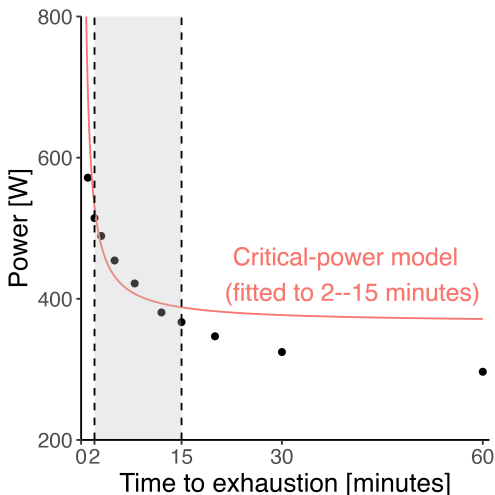


Figure: Fits reasonably when applied to 2–15 minutes

Hyperbolic/Critical-power vs Power-law model

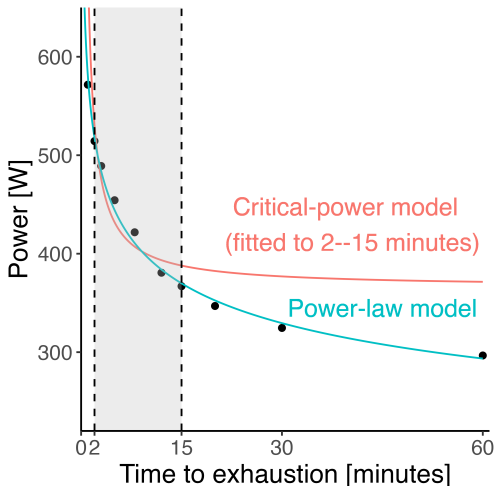
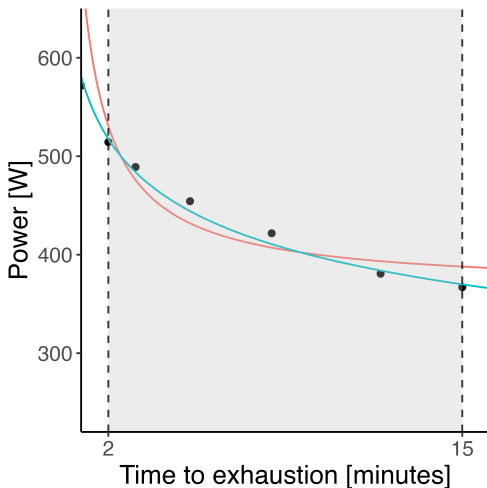
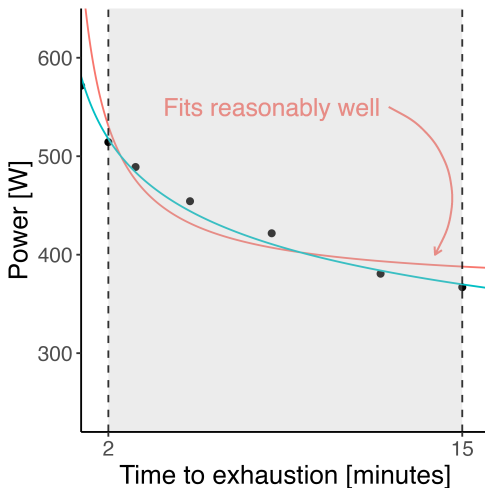


Figure: Power-law model fits better

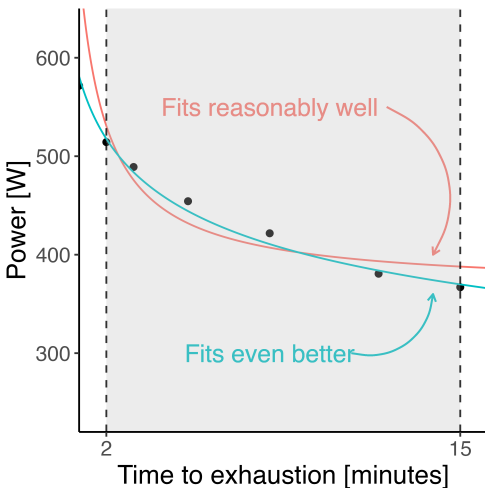
Medium durations



Medium durations



Medium durations



Short durations

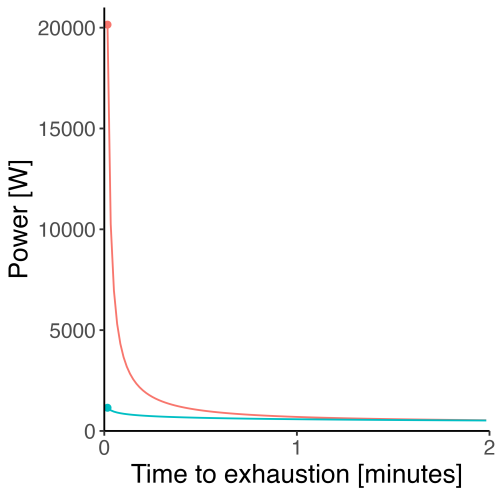


Figure: Power sustainable over 1 second

Short durations

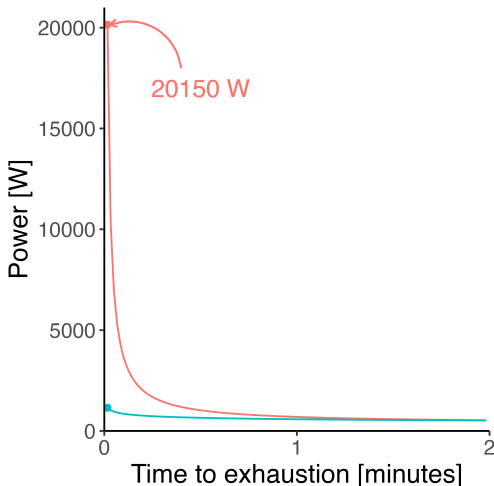


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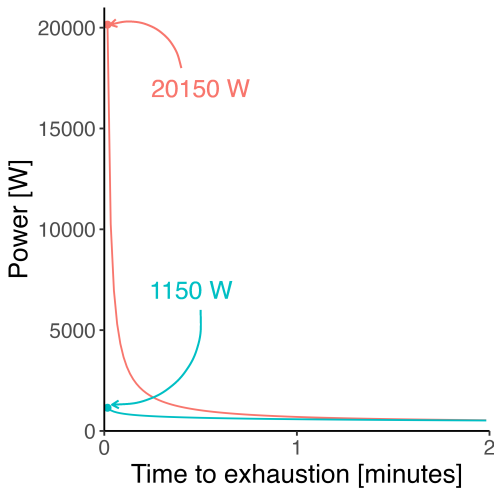


Figure: Power sustainable over 1 second

Long durations

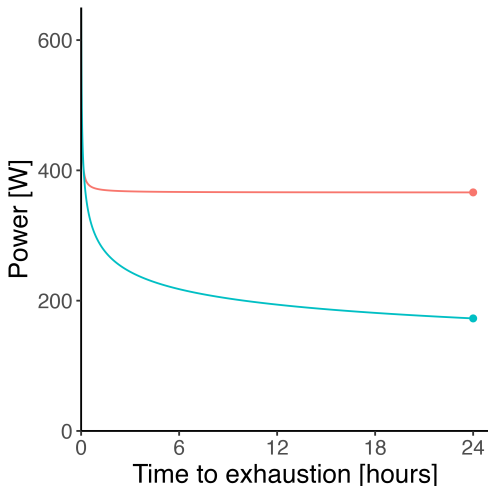


Figure: Power sustainable over 24 hours

Long durations

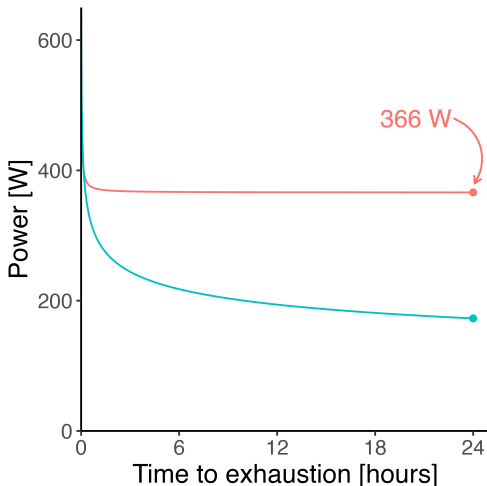


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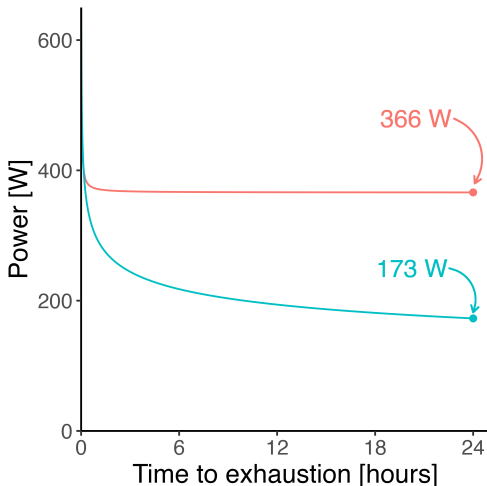
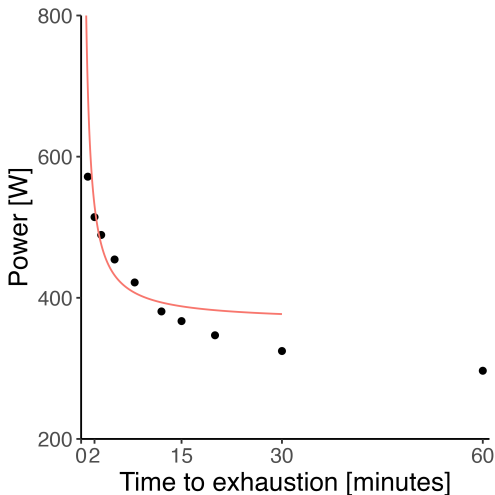
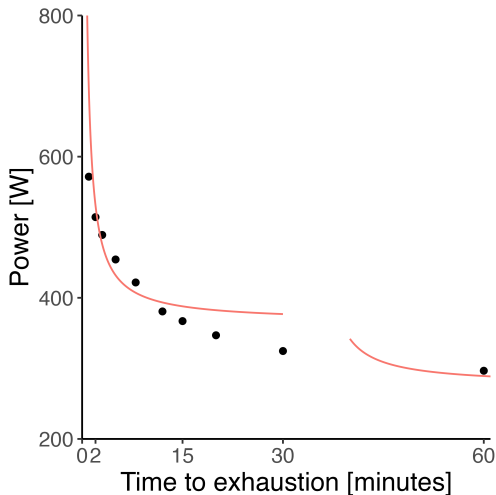


Figure: Power sustainable over 24 hours

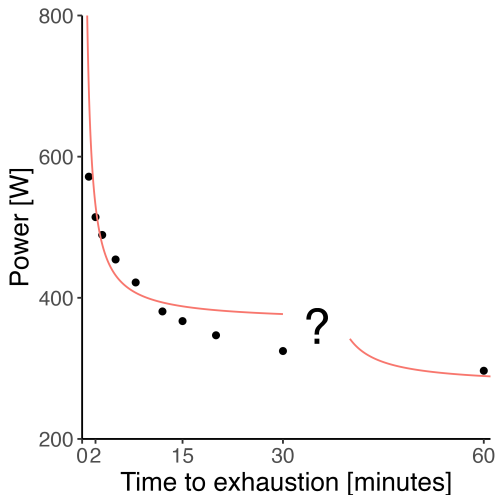
What do we think happens?



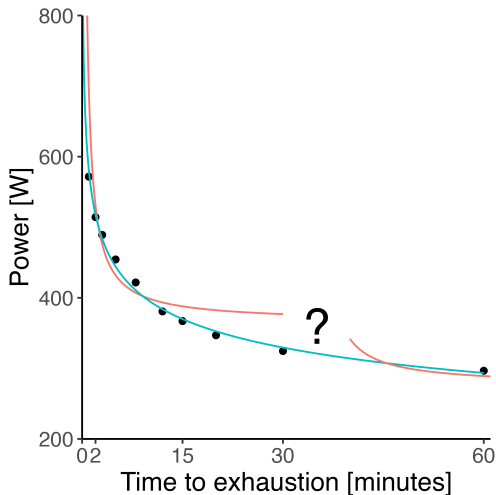
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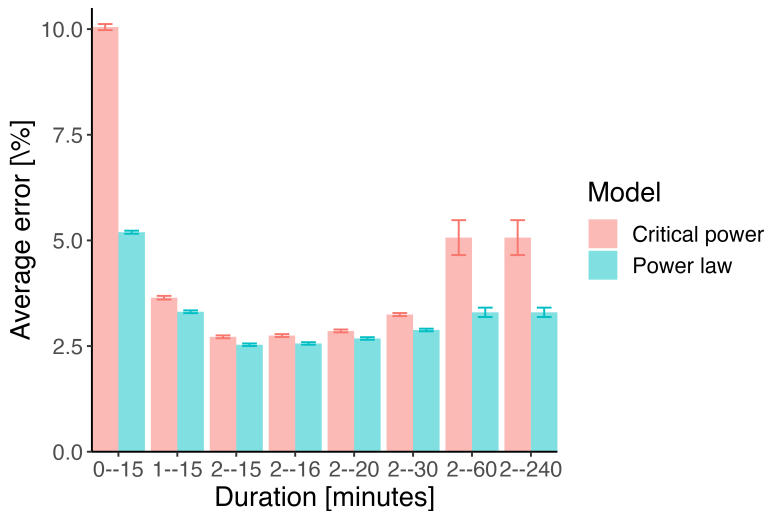


Figure: Large data study of 5805 cyclists

Cycling

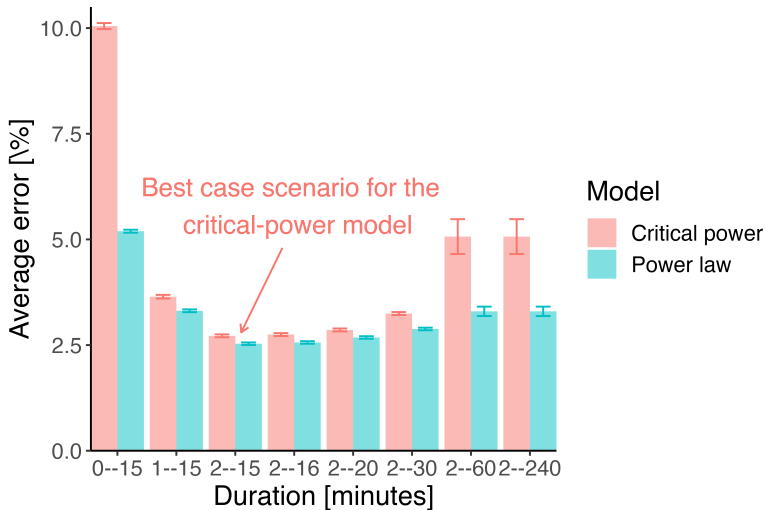


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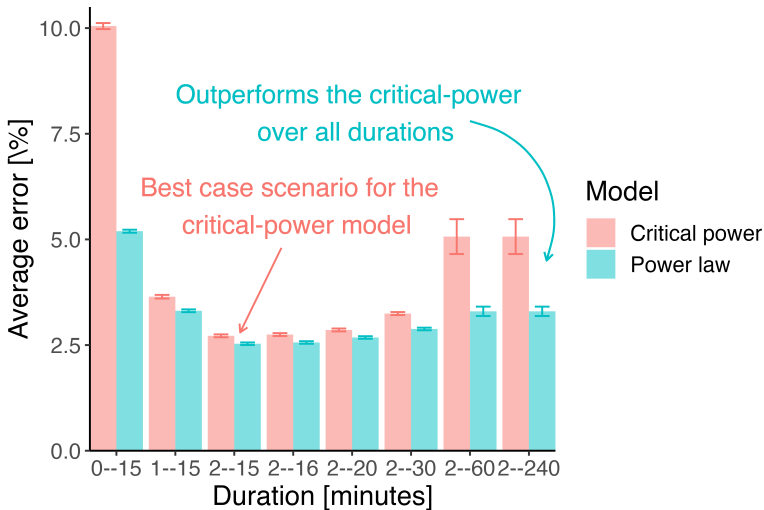


Figure: Large data study of 5805 cyclists

Running

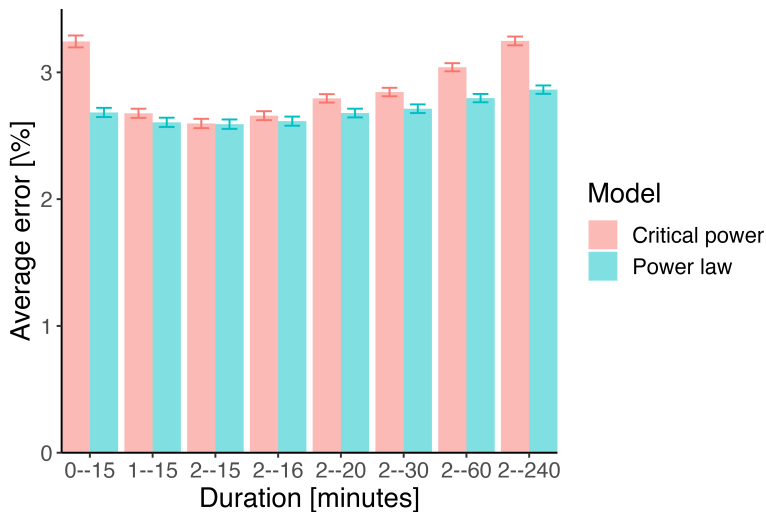


Figure: Large data study of 2571 runners

Rowing

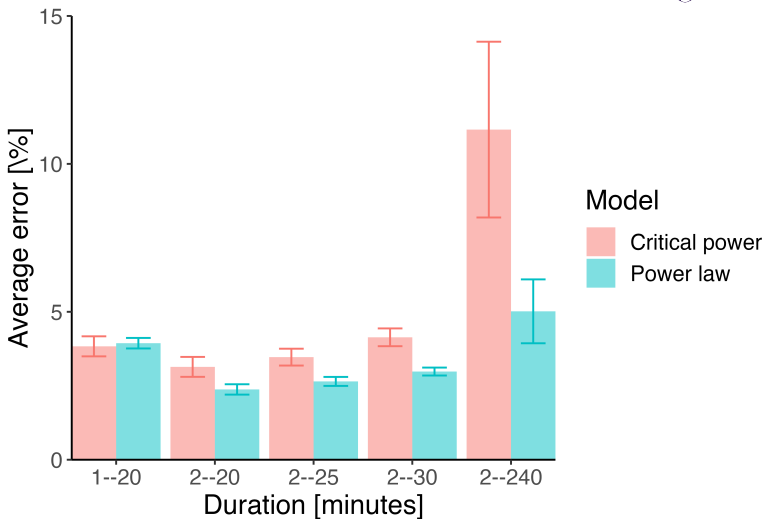


Figure: Large data study of 3244 rowers

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Takeaways



The power-law model...

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- ▶ more accurately predicts performance than CP/W' over a **wide range of durations**,

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Summary

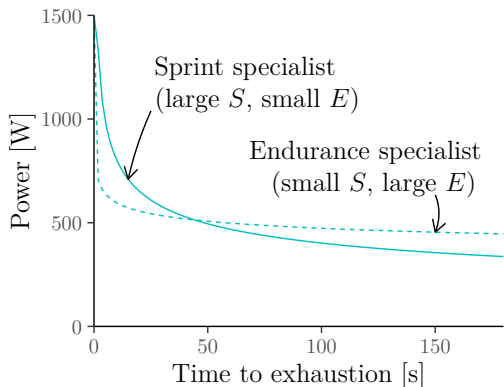
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Speed, $S > 0$, in cycling the theoretical 1 second power output

Endurance, $0 < E < 1$, governs how quickly the power–duration curve decays



Riegel (1981)

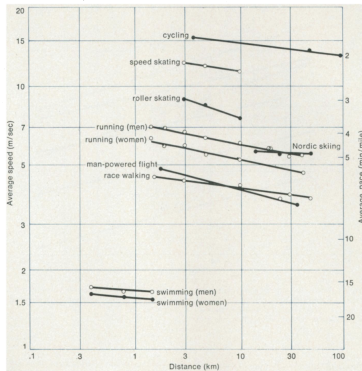


Figure: World records **across different athletes** from multiple sports (Riegel, 1981)

Estimated the endurance parameter to be $E \approx 0.953889$

Connecting FTP

FTP - Originally defined as 1 hour power (Allen and Coggan, 2012)

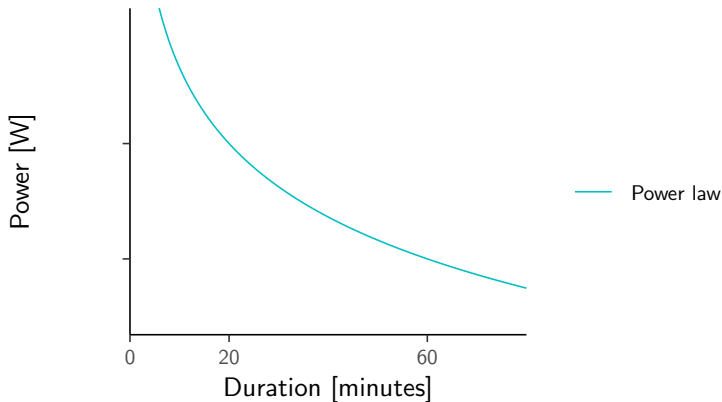
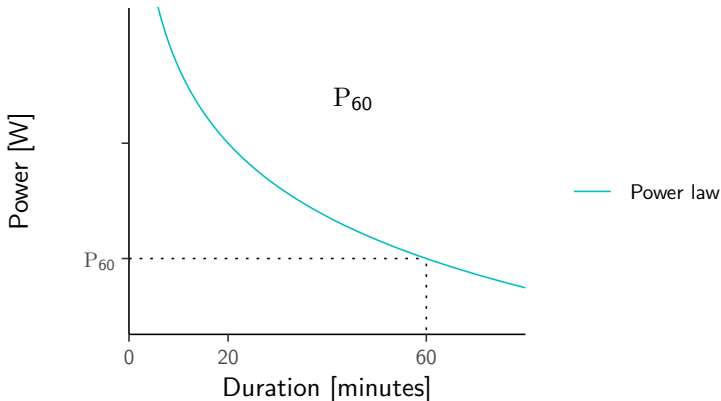


Figure: Power-duration curve from Riegel (1981)

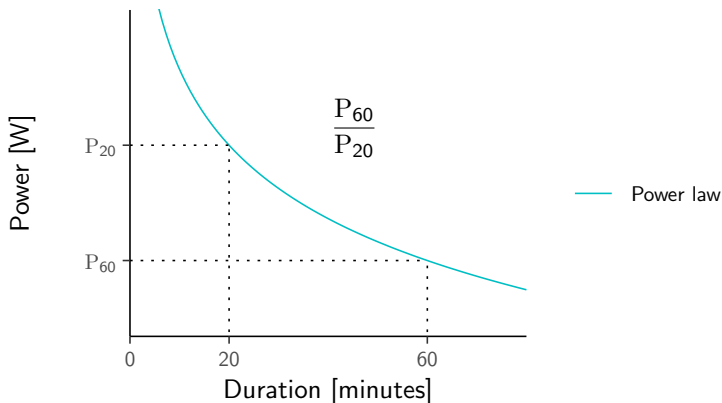
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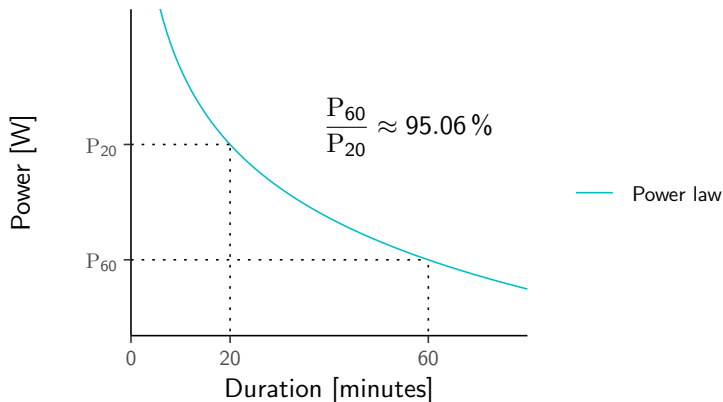
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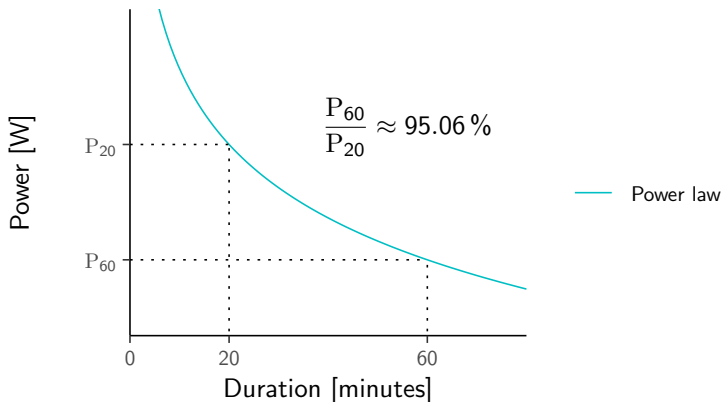
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Exactly the rule used to estimate FTP

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The power-law model...

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- ▶ is just as **easy to use**,
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The power-law model...

- ▶ more accurately predicts performance than CP/W' over a **wide range of durations**,
- ▶ is just as **easy to use**,
- ▶ can use the **same testing protocols** as CP/W'
- ▶ explains why the 95 % rule for **FTP is typically an overestimate**

Limitations



The power-law model **can not** explain...

Limitations



The power-law model **can not** explain...

- ▶ **recovery**

Limitations

The power-law model **can not** explain...

- ▶ **recovery**
- ▶ **slowdown**

References I



Hunter Allen and Andrew Coggan. *Training and racing with a power meter*. VeloPress, 2nd edition, 2012.

Archibald Vivian Hill. The physiological basis of athletic records. *The Scientific Monthly*, 21(4):409–428, 1925.

Andrew M Jones, Mark Burnley, Matthew I Black, David C Poole, and Anni Vanhatalo. The maximal metabolic steady state: re-defining the 'gold standard'. *Physiological Reports*, 7(10):e14098, 2019.

Arthur Edwin Kennelly. An approximate law of fatigue in the speeds of racing animals. *Proceedings of the American Academy of Arts and Sciences*, 42(15):275–331, 1906.

H Monod and J Scherrer. The work capacity of a synergic muscular group. *Ergonomics*, 8(3):329–338, 1965.

Peter S Riegel. Athletic records and human endurance. *American Scientist*, 69(3):285–290, 1981.